

Quantum Plasmonic Sensing: Beyond the Shot-Noise and Diffraction Limit

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S Supporting Information

[AB](#page-5-0)STRACT: [Photonic sens](#page-5-0)ors have many applications in a range of physical settings, from measuring mechanical pressure in manufacturing to detecting protein concentration in biomedical samples. A variety of sensing approaches exist, and plasmonic systems in particular have received much attention due to their ability to confine light below the diffraction limit, greatly enhancing sensitivity. Recently, quantum techniques have been identified that can outperform classical sensing methods and achieve sensitivity below the so-called shot-noise limit. Despite this significant potential, the use of definite photon number states in lossy plasmonic systems for further improving sensing capabilities is not well studied. Here, we investigate the sensing performance of a plasmonic interferometer that simultaneously exploits the quantum

nature of light and its electromagnetic field confinement. We show that, despite the presence of loss, specialized quantum resources can provide improved sensitivity and resolution beyond the shot-noise limit within a compact plasmonic device operating below the diffraction limit.

KEYWORDS: plasmonic sensing, quantum metrology, quantum plasmonic sensing

Plasmonic excitations have attracted enormous interest in recent years from a variety of scientific fields due to their intriguing light-matter features and wide range of applications.1,2 Plasmonic biosensing, in particular, is one of the most successful applications, with devices that outperform conventiona[l on](#page-6-0)es that rely on ordinary photonic components.^{3–5} Due to their high sensitivity, multiple surface plasmon resonance (SPR) sensing devices have been developed o[v](#page-6-0)e[r](#page-6-0) the decades.6−¹³ The higher sensitivity of SPR sensors is achieved via a strong electromagnetic (EM) field enhancement at a metal surface, [wher](#page-6-0)e its interaction with free electrons forms a surface plasmon that confines the field to a spatial domain below the $diffraction$ limit. 14 Such confinement is not possible with ordinary dielectric media.¹⁵ Despite their practical realization and successful [co](#page-6-0)mmercialization, the high sensitivity and associated resolution of S[PR](#page-6-0) sensing are fundamentally limited by the discretized nature of light known as the shot-noise limit $(SNL).$ ¹⁶ However, recently it has been shown that the SNL can be beaten by using quantum states of light having a superor sub-[Po](#page-6-0)issonian photon distribution, or intermode entanglement, 17 and an appropriate type of measurement, a strategy

known as quantum metrology.¹⁸ A number of impressive experiments have already demonstrated the basic working features of quantum metrology u[sin](#page-6-0)g multiphoton states in bulk optics,^{19−23} integrated optics,²⁴ and sensing biological systems.^{25,26} A question naturally arises about whether such quantu[m](#page-6-0) [tec](#page-6-0)hniques could be e[mpl](#page-6-0)oyed in plasmonic sensors in order [to f](#page-6-0)urther enhance their capabilities. Here, absorption constitutes a significant challenge that usually causes a degradation of the quality of a quantum resource.²

Very recently, work has shown the possibility of reducing quantum noise in plasmonic sensing by using [a](#page-6-0) two-mode quadrature squeezed state in a prism configuration^{28,29} and in a nanoparticle array.³⁰ However, the role of quantum effects in more general plasmonic sensing devices at the few[-pho](#page-6-0)ton level is not well unde[rsto](#page-6-0)od. To address this, we begin with a concept of quantum plasmonic sensing that utilizes both quantum features of resource states at the few-photon level and the EM field enhancement offered by plasmonic structures. We

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show how the combination of quantum and plasmonic aspects enables one to improve the sensitivity of a device beyond the SNL, while keeping its compactness on scales below the diffraction limit. We highlight the feasibility of our approach by examining the minimum resolution of parameter estimation in an example interferometer-based plasmonic biosensor. Here, we consider waveguides that have numerous attractive features geared toward the design of compact, mobile, broadband and integratable biosensors. Our analysis shows the beneficial role that quantum effects can play in a plasmonic sensor, despite the presence of loss. The techniques developed can be applied to many other plasmonic sensing platforms and thus we expect this work to stimulate a variety of further investigations beyond conventional quantum metrology and classical plasmonic sensing. 31

■ C[ON](#page-6-0)CEPT OF QUANTUM PLASMONIC SENSING

We begin with the general scenario for photonic sensing shown in Figure 1a, which is divided into three stages: (i) a signal preparation where an incident light field is prepared, (ii) a transducer that encodes the information on the parameter to be measured onto the output signal, and (iii) a measurement that analyzes the output signal from the transducer. A biological setting is chosen as an example, where a physicochemical transducer encodes the information of surrounding biological objects onto the output signal. For other settings the transducer may take a different form, such as for mechanical,³²⁻³⁴ electrical,³⁵ or magnetic parameters.^{36,37} In the classical

Figure 1. General scenario for photonic sensing. (a) For a properly chosen signal, one measures and analyzes the output light from a transducer. An example of a biosensor is given, where the transducer encodes onto the light signal changes in the biological medium. (b) Four regions in which photonic sensing devices operate, distinguishing the use of quantum or classical techniques in the signal and measurement parts, and the use of dielectric or plasmonic material in the transducer part. The enhancement of sensitivity has been known to be achieved through the yellow arrows, whereas there is an intriguing region in the top right that has recently begun to attract attention, called quantum plasmonic sensing. $28-31$

measurement scenario, a classical source is used for the input signal, a dielectric medium represents the transducer and a classical intensity measurement is performed. An enhancement of sensitivity can be obtained here via two directions: First, plasmonic effects can be employed in the transducer by using a metallic medium providing a strong EM field enhancement. This enables a much higher sensitivity compared to the field in a conventional dielectric medium, as a change of environment produces a larger change of the mode properties of surface plasmons compared to photons. $3-5$ Second, the signal and measurement parts can be replaced by quantum elements. For example, it has been shown th[at s](#page-6-0)tates known as NOON states 38 or quadrature-squeezed states¹⁶ can improve the minimum resolution of parameter estimation beyond the SNL [by](#page-6-0) using an appropriate measur[em](#page-6-0)ent scheme. Such quantum strategies have been employed for biosensing recently to minimize the shot-noise associated with the random arrival of photons at a detector.^{26,39} Even more recently, the use of plasmonic elements has begun to be considered with the above quantum strategies, sho[wing](#page-6-0) the capability of beating the SNL.28−³⁰ However, it is not entirely clear how quantum techniques can be incorporated into plasmonic sensing for furth[er im](#page-6-0)proving the sensitivity with finite photon number states, even though it has been demonstrated that properties such as quantum coherence can be preserved in plasmonic systems.^{40−43} It is nontrivial that sensitivity beyond the SNL is achievable in such a lossy, open quantum system. As we will show, q[uantu](#page-7-0)m plasmonic sensing is complementary to both classical plasmonic and quantum techniques for improving the sensitivity of photonic sensors, as depicted in Figure 1b. However, the key merit is that it improves functionality by beating the SNL in a subdiffraction scale system.

■ RESULTS

Simulation. We illustrate the basic concept of quantum plasmonic sensing in Figure 2a, where a two-arm interferometer, one of the most successful photonic sensing techniques, ^{9,44,45} is e[mployed w](#page-2-0)ith a nanowire waveguide in one arm. We focus on a nanowire structure initially as it is a well studie[d](#page-6-0) [geo](#page-7-0)metry with many applications in plasmonic circuitry46,47 and has a high level of miniaturization for sensing with an accessible interrogation area. 3 The interferometric sensor [cons](#page-7-0)ists of source and measurement parts and a transducer part for one arm. The tr[an](#page-6-0)sducer consists of a dielectric or metallic nanowire with refractive index $n_d = 1.4475$ (doped silica) or $n_m(\omega) = \sqrt{\epsilon_m(\omega)}$ (silver) given by experimental data,⁴⁸ respectively. The nanowire is surrounded by a biological medium with refractive index n_{bio} , whose value varies due to ch[an](#page-7-0)ges in the concentration of a biological analyte. We choose a range for n_{bio} that ensures single-mode operation in the waveguides (see Supporting Information). The change in the biological medium changes the wavenumber k of the waveguide mode, and the [change of the wavenu](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)mber changes the relative accumulated phase of the fields, ϕ , between both arms, which can be measured in the output signal via an interference measurement. Here, the wavenumber k for dielectric and metallic nanowires is determined by a characteristic equation^{15,49,50} (see Supporting Information). From the measurement, we aim to estimate the refractive index unit (RIU) n_{bio} wi[th](#page-6-0) [the](#page-7-0) small[est detectable refractive in](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)dex change δn_{bio} assuming for simplicity that there is no scattering when the input signal enters into the sensing region in the first arm.

Figure 2. Quantum plasmonic sensing. (a) General two-mode interferometer with one arm in a nanowire waveguide. A quantum or classical state from a source stage is fed into the interferometer. The sensing arm (mode 1) is embedded in an environment and the signal acquires a phase change $\Delta\phi$ due to changes in the refractive index, n_{bio} , during its propagation, modifying the output signal at the measurement stage. (b) The expectation values of an observable $\langle \hat{O} \rangle$, where $\hat{O} = \hat{M}$ (with $|\psi_{\text{out}}\rangle_{\text{classical}}$) and \hat{A} (with $|\psi_{\text{out}}\rangle_{\text{quantum}}$), optimized for classical (C) and quantum (Q) sensors, respectively. Here, an average photon number of $N = 4$ is used to show that the quantum plasmonic case (the red curve) oscillates more rapidly than all others, implying that a small change of n_{bio} induces a large detectable change in the monitored output signal. In this example, we consider both dielectric and lossless silver metallic nanowires, with a core radius of 50 nm and a length of $l = 4 \mu$ m at $\lambda_0 = 810$ nm, where $n_{\text{core}} = 1.4475$ and $n_{\text{core}}(\omega) = \sqrt{\epsilon_{\text{m}}(\omega)}$ from the experimental data in ref 48. (c) The minimum resolution, δn_{bio} , shows that quantum plasmonic sensing exhibits the best performance.

A reference point for classical sensing can [be](#page-7-0) found by considering the entire device as a Mach−Zehnder (MZ) interferometer. Here, a coherent state $|\alpha\rangle$, written in the Fockstate basis $|m\rangle$ as

$$
|\alpha\rangle = e^{-|\alpha|^2/2} \sum_{m=0}^{\infty} \frac{\alpha^m}{\sqrt{m!}} |m\rangle
$$
 (1)

with mean photon number, $|\alpha|^2 = N$, is fed into one input port of the first beamsplitter of the MZ and a vacuum state fed into the other. The output of this beamsplitter constitutes the source stage. An intensity-difference measurement, $\hat{M} = \hat{I}_1 - \hat{I}_2$, is performed by using the second beamsplitter of the MZ placed after the sensing region and measuring the output intensities. This constitutes the measurement stage. The above classical sensing strategy is optimal in that it leads to the SNL on the resolution δn_bio .

On the other hand, by using quantum techniques, one can consider a NOON state^{22,23,51} generated at the source stage, that is,

$$
|\psi_{\text{in}}\rangle = \frac{1}{\sqrt{2}} (|N0\rangle_{12} + |0N\rangle_{12})
$$
 (2)

where N denotes the number of photons. The observable $\hat{A} = |0, N\rangle\langle N, 0| + |N, 0\rangle\langle 0, N|$ can be used for the quantum measurement, which together with the NOON state allows one to reach the Heisenberg limit (HL) for $\delta n_{\rm bio}$ in the absence of photon loss.^{18,2}

In Figure 2b, we present the measurement signals $\langle \hat{M} \rangle = M_0$ $cos(\phi(n_{\text{bio}}))$ and $\langle \hat{A} \rangle = A_0 cos(N\phi(n_{\text{bio}}))$ simulated for the classical scenario using a coherent state and the quantum scenario using a NOON state, respectively. The state $|\psi_{\text{out}}\rangle$

generated from encoding ϕ onto the input state $|\psi_{in}\rangle$ is used to calculate $\langle \ldots \rangle$, that is,

$$
|\psi_{\text{out}}\rangle_{\text{classical}} = |\frac{1}{2}\alpha(e^{i\phi} - 1)\rangle_1 |\frac{1}{2}i\alpha(e^{i\phi} + 1)\rangle_2
$$

and

$$
\left|\psi_{\text{out}}\rangle_{\text{quantum}} = \frac{1}{\sqrt{2}} \left(e^{IN\phi} \middle| N0 \right)_{12} + \left| 0N \right\rangle_{12} \right)
$$

(see Supporting Information). Here, $N = 4$ has been chosen and $\phi(n_{\text{bio}})$ denotes the relative phase accumulated during prop[agation \(free-space wave](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)length $\lambda_0 = 810$ nm chosen as an example) along a dielectric and silver nanowire with a core radius of 50 nm and length $l = 4 \mu m$. The lateral confinement of the field of the dielectric nanowire is diffraction limited $({\sim}\lambda_0/n_d)$, whereas that of the metallic nanowire is not $({\ll}\lambda_0)$.¹⁵ For the relative phase picked up, we have $\phi(n_{\text{bio}}) = \beta(n_{\text{bio}}) \times l$, where the propagation constant $\beta(n_{\text{bio}}) \equiv \text{Re}[k]$ is a function [of](#page-6-0) n_{bio} (see Supporting Information). Here, we have considered a lossless silver nanowire, that is, $Im[k] = 0$. We consider the impact o[f losses later. The main p](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)urpose at this stage is to show the difference between classical and quantum techniques, and the use of dielectric and plasmonic systems. It can be seen in Figure 2b that the expectation value for the quantum plasmonic case oscillates far more rapidly than the others, implying that a small change of n_{bio} induces a large detectable change of the measurement signal. It may seem like one can resolve an infinitesimal change of n_{bio} by simply measuring the change of a given measurement signal, but this is not the case as the curves in Figure 2b become naturally blurred when quantum fluctuations are involved. Therefore, in Figure 2c we evaluate the minimum resolution of the refractive index change

achievable from an observable \hat{O} (= \hat{A} or \hat{M} for quantum or classical scenarios) with quantum fluctuations included. The resolution is obtained by the linear error propagation method 52 as

$$
\delta n_{\rm bio} = \frac{\Delta \hat{O}}{|\partial \langle \hat{O} \rangle / \partial n_{\rm bio}|} \tag{3}
$$

where $\Delta \hat{O} = (\langle \hat{O}^2 \rangle - \langle \hat{O} \rangle^2)^{1/2}$. Here, the parameter of interest in our biosensing scenario is $n_{\rm bio}$ instead of the relative phase $\phi,$ the usual quantity considered in quantum metrology.¹⁸ Its corresponding resolution $\delta n_{\rm bio}$ depends on the waveguide material. The behaviors seen in Figure 2c clearly show t[hat,](#page-6-0) for the quantum plasmonic case, the resolution $\delta n_{\rm bio}$ is smallest compared to the others. This i[mplies th](#page-2-0)at quantum plasmonic sensing can outperform both standard dielectric quantum metrology and classical plasmonic sensing within the same parameter regime. We note that the quantum case yields a material-dependent HL, $\delta n^{(\text{HL})}_{\text{bio}} = \frac{1}{N} \left| \frac{\partial \phi}{\partial n_{\text{bio}}} \right|$ − $n_{\text{bio}}^{\text{(HL)}} = \frac{1}{N} \left| \frac{\partial \phi}{\partial n_{\text{bio}}} \right|^{-1}$ $\frac{\partial \psi}{\partial \rho}$, which has a factor \sqrt{N} improvement over the classical case with a materialdependent SNL, $\delta n_{\textrm{bio}}^{(\textrm{SNL})} = \frac{1}{\sqrt{N}} \bigg| \frac{\partial \phi}{\partial n_{\textrm{bio}}}$ − $n_{\text{bio}}^{(\text{SNL})} = \frac{1}{\sqrt{N}} \left| \frac{\partial \phi}{\partial n_{\text{bio}}} \right|^{-1}$ $\frac{\varphi}{\text{bio}}$, the origins of which we discuss in detail below.

Quantum and Plasmonic Features Combined for Enhanced Sensing. We now look at how quantum resources enable plasmonic sensing to go beyond the SNL. The interferometric setup in Figure 2a has the ability to quantitatively detect a phase change $\Delta \phi$ induced by a change of the propagation constant, [that is,](#page-2-0) $\Delta \phi = \Delta \beta \times l$, where $\Delta \beta$ is induced by a variation in the analyte. Thus, the chosen material in the transducer is only responsible for how sensitively it accumulates $\Delta \phi$ as n_{bio} changes. On the other hand, the quantum source and measurement are responsible for how sensitively the chosen state and measurement stage respond to $\Delta \phi$. Such separate roles are manifested in the *sensitivity*, defined as the ratio of the change in sensor output $\langle \hat{O} \rangle$ to the change in n_{bio} , which can be written by the chain rule as

$$
S = \frac{\partial \langle \hat{O} \rangle}{\partial n_{\text{bio}}} = \frac{\partial \langle \hat{O} \rangle}{\partial \phi} \frac{\partial \phi}{\partial n_{\text{bio}}} \tag{4}
$$

where the expectation value $\langle \hat{O} \rangle$ is assumed to have only ϕ dependence with respect to n_{bio} . The first term on the righthand side describes the sensitivity of the output $\langle \hat{O} \rangle$ to ϕ , whereas the second term describes the sensitivity of ϕ to n_{bio} . Consequently, eq 3 can be rewritten as

$$
\delta n_{\rm bio} = \delta \phi \left| \frac{\partial \phi}{\partial n_{\rm bio}} \right|^{-1} \tag{5}
$$

where $\delta \phi = \Delta \hat{O} / |\partial \langle \hat{O} \rangle / \partial \phi|$ denotes the minimum resolution of the phase and does not depend on the waveguide material, provided that $|\psi_{\text{out}}\rangle$ can be written as a function of ϕ only. Note that it is the nonclassical nature of the source and the measurement that decreases $\delta \phi$ below the SNL, which is clearly seen in Figure 3a,b, where we reproduce well-known behaviors of $\langle \hat{O} \rangle$ and $\delta \phi$ for classical and quantum metrology with the same input states and measurements used in Figure 2. On the other hand, the sensitivity $\partial \phi / \partial n_{\text{bio}}$ (=l × $\partial \beta / \partial n_{\text{bio}}$) depends on the material used and can be increased [by a pl](#page-2-0)asmonic transducer. In Figure 3c,d, we show β and its slope change with increasing RIU for dielectric and metallic waveguides. The enhanced sensitivity of β is a result of the strong field

Figure 3. Roles of quantum and plasmonic effects. Quantum-enhanced sensitivity comes from the source and measurement stages, which are responsible for how sensitive the initial state and the observable are with respect to the phase. (a) Comparison of the classical and quantum metrology scenarios in terms of the expectation values of Â and \hat{M} . (b) Minimum estimation precision, $\delta\phi$, corresponding to the measurements in panel (a). In panel (a), the expectation value of $\langle \hat{A} \rangle$ oscillates more rapidly than that of $\langle \hat{M} \rangle$; the classical case leads to the SNL and the quantum case leads to the HL in panel (b), that is, $\delta\phi^{\text{(SNL)}} = 1/\sqrt{N}$ and $\delta\phi^{\text{(HL)}} = 1/N$. The plasmonic enhanced sensitivity comes from the transducer, which can be seen in terms of the relation between the propagation constant β and n_{bio} . (c) β for the lossless plasmonic and dielectric waveguides. (d) Slope of β over n_{bio} showing the rate of change.

confinement for the plasmonic mode, making it more sensitive to Δn_{bio} . In other words, the resolution $\delta \phi$ is improved by properties of a chosen input state and measurement, while the sensitivity $\partial \phi / \partial n_{\text{bio}}$ is improved by the mode properties of the transducer. The combined effect of these quantum and plasmonic features is what leads to the results seen in Figure 2c.

Our analysis can be generalized to any kind of plasmonic setup for which the sensitivity and the minimum reso[lution ca](#page-2-0)n be rewritten in terms of a parameter X as $\tilde{S} = \frac{\partial \langle \hat{O} \rangle}{\partial x}$ ∂ $\tilde{S} = \frac{\partial \langle \tilde{O} \rangle}{\partial X} \frac{\partial}{\partial n}$ *X* $\frac{\partial A}{\partial n_{\rm bio}}$ and $\delta \tilde{n}_{\rm bio} = \delta X \left| \frac{\partial}{\partial n} \right|$ $\tilde{n}_{\rm bio} = \delta X \left| \frac{\partial X}{\partial n_{\rm bio}} \right|^{-1}$ 1 $\frac{X}{\delta}$, where $\delta X = \Delta \hat{O}/|\partial \langle \hat{O} \rangle / \partial X|$ denotes the

minimum resolution of parameter estimation. The enhancement of $\partial X/\partial n_{\text{bio}}$ depends on the material, the modulation technique, and the surface plasmon excitation method.⁵³ On the other hand, $\partial \langle \hat{O} \rangle / \partial X$ and δX depend on the quantum input $|\psi_{\text{in}}\rangle$ and the measurement \hat{O} , where the [out](#page-7-0)put $|\psi_{\text{out}}\rangle$ is generated from encoding X onto the input $|\psi_{\text{in}}\rangle$. For example, the widely used Kretschmann configuration could replace the transducer shown in Figure 1a 28,29 and the reflection coefficient $|R|^2$ used as the effective parameter X. In this case, the refractive index change would [not be p](#page-1-0)i[cked](#page-6-0) up as a phase, but rather as an intensity (or peak angular position). However, one could also consider embedding the Kretschmann configuration directly within an interferometer,⁵⁴ and the change picked up as a phase, bringing this method inline with the interferometric setting we have described. The[se](#page-7-0) more general expressions provide a better understanding of the specific roles that quantum and plasmonic features play and enable the efficient optimization of quantum plasmonic sensing. In addition to enhanced sensitivity and resolution, there are other advantages of using plasmonics, for example, a small-sized mode volume below the diffraction limit that conventional photonics cannot achieve. This is important since a highly miniaturized sensor is commonly required to measure tiny organic molecules within a limited interaction area. 3 The combination of the reduced shotnoise of a quantum resource and the enhanced sensitivity provided by plasmonics guarantees that quantum plasmonic sensing can, in principle, go beyond both the shot-noise and the diffraction limit.

Realistic Scenario Including Loss. We now show that quantum plasmonic sensing remains able to beat the SNL even when realistic metallic losses are included. To do this, we require an optimal quantum state for the source for a given amount of loss. The NOON state previously studied is extremely fragile to loss and is not an optimal quantum state, resulting in a much worse resolution than the SNL even for moderate loss.⁵⁵ Assuming the optimal measurement will be performed, we focus on optimizing the input state. In this case, the minimum [re](#page-7-0)solution is given by the Cramer-Rao bound according to quantum parameter estimation theory,⁵⁶ that is,

$$
\delta \phi = F_Q^{-1/2} \tag{6}
$$

where the quantum Fisher information, F_{Q} , represents a measure of the amount of information that a state contains about ϕ with respect to the optimized measurement over all possible schemes (see Supporting Information). We optimize the coefficients of an input state with fixed N written as

$$
|\psi_{\text{in}}\rangle = \sum_{n=0}^{N} c_n |n, N - n\rangle \tag{7}
$$

such that F_Q is maximized and $\delta\phi$ is minimized.⁵⁵

As possible plasmonic waveguides, we consider the nanowire w[ave](#page-7-0)guide previously studied and a wedge waveguide, 57 as shown in Figure 2a. Wedge waveguides have recently been shown to be highly beneficial for plasmonic devices i[n](#page-7-0) the quantum [regime du](#page-2-0)e to their high field confinement⁵⁸ and broadband response over a wide operating range, a key requirement for a good biosensor, allowing one to [a](#page-7-0)void frequencies where the analyte is absorbing. The amount of loss in the waveguides is determined by Im[k] and l, with $l = 4 \mu m$ chosen as an example. We use a beamsplitter model for including loss, where a fictitious beam splitter with a transmitivity $\eta = \exp(-2\text{Im}[k]l)$ is inserted in one arm of the interferometer. Such a model is also valid for loss occurring during the phase acquisition in a metallic nanowire since the loss operation and the phase accumulation commute with each other.⁵⁵ The parameter F_Q is then given as a function of the set $\{x_n = |c_n^2|\}$ and η (see Supporting Information). For the nano[wir](#page-7-0)e, we consider the same range of n_{bio} as before in order to aid comparison of the [results. On the other ha](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)nd, for the refractive index near the wedge waveguide, in order to give a more realistic scenario, we consider $n_{\text{bio}} = n_s + A \times C$, where n_s $= 1.333$ denotes water as a solvent, $A = 0.00182$, and C represent Bovine Serum Albumin (BSA) as a solute¹³ and the number of grams of BSA solute per 100 mL of solution, respectively. For the wedge waveguide, C is varied [fro](#page-6-0)m 0 to 60%, yielding n_{bio} ranging from 1.333 to 1.4422. For the nanowire, n_{bio} is between 1.1 and 1.4 as before, ensuring that only a single mode exists for a radius of 50 nm. For the wedge waveguide, the top angle is 70.6° and the bottom angles are 54.7° (see Supporting Information). The plasmon mode sits on top of the wedge, and the height can be set arbitrarily small down to ~50 nm for λ_0 = 810 nm, after which the mode has a significant [presence](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf) [at](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf) [the](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf) [bottom](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf) edges. $57,58$

For the respective ranges of n_{bio} , we present the transmission coefficient η in Figure 4a,b. For each η , [depen](#page-7-0)ding on n_{bio} , the optimal distributions of $\{x_n\}$ for $N = 4$ are shown in Figure

Figure 4. Realistic quantum plasmonic sensing. A lossy nanowire (left column) and a wedge waveguide (right column) are considered, where loss is modeled as a fictitious beamsplitter with a transmitivity η = $\exp(-2\text{Im}[k]l)$ for a propagation length l. (a) For propagation with l = 4 μ m, η is obtained in terms of n_{bio} by solving the characteristic equation for the nanowire.^{15,49} (b) FEM simulation via COMSOL is used for the wedge waveguide (top angle 70.6° and bottom angles 54.7°). (c) The optimal s[et](#page-6-0) $\{x_n\}$ for a state with a definite photon number $N = 4$ is shown for the nanowire waveguide. (d) The optimal set $\{x_n\}$ for the wedge waveguide. (e) The optimal resolution imposed by the Cramér-Rao bound for the NOON state and the optimized state for a given η for the nanowire. (f) The optimal resolution for the wedge waveguide. The shaded area in panels (e) and (f) is bounded at the top by the standard interferometric limit (SIL), corresponding to the SNL but optimized for an unbalanced beamsplitter to minimize the resolution in the presence of losses.⁵⁹ The area is bounded at the bottom by the HL. A line within the shaded area shows an improvement over classical plasmonic [sen](#page-7-0)sing.

4c,d, for which F_Q is maximized, yielding the optimal minimum resolutions in Figure 4e,f. The optimal x_n coefficients define the "optimal state" for sensing and are different depending on the amount of loss, but their relative phases are not important.⁵⁵ We also compare the optimal minimum resolutions with the HL (lower dashed lines) and the standard interferometric li[mit](#page-7-0) (SIL) (upper dashed lines), which corresponds to the SNL, but optimized using an unbalanced beamsplitter in order to minimize resolution in the presence of losses.⁵⁹ It can be clearly seen that the resolution with the NOON state is much worse than the SIL given as

$$
\delta n_{\text{bio}}^{(\text{SIL})} = \frac{1 + \sqrt{\eta}}{2\sqrt{N\eta}} \left| \frac{\partial \phi}{\partial n_{\text{bio}}} \right|^{-1} \tag{8}
$$

whereas the optimal state beats the SIL in both plasmonic waveguides.

The optimal state is different depending on the amount of loss, so for experimental relevance it is important to check if a given input state optimized for a certain amount of loss still beats the SIL over the whole range of n_{bio} measured. Figure 5a and b present the results of three points chosen from Figure 4c and d, respectively, showing that the chosen stat[es remain](#page-5-0) beyond the SIL over the respective ranges of n_{bio} .

Figure 5. Resolutions of optimal states and increasing average number of photons. Input states optimized for a certain amount of loss still beat the SIL over the whole range of n_{bio} for the lossy plasmonic nanowire and wedge waveguides considered in Figure 4. (a) Three points are randomly chosen from Figure 4c: (1) $n_{\text{bio}} = 1.13$, (2) $n_{\text{bio}} =$ 1.19, and (3) $n_{\text{bio}} = 1.37$. For these points, the optimal states found with the corresponding amount of loss are used a[s the inpu](#page-4-0)t states and the resolutions are obtained ov[er the w](#page-4-0)hole range of n_{bio} for the nanowire waveguide. (b) Same as (a), but for the wedge waveguide. Here the points correspond to those in Figure 4d: (1) $n_{\text{bio}} = 1.34392$, (2) $n_{\text{bio}} = 1.36576$, and (3) $n_{\text{bio}} = 1.43128$. (c) The resolution δn_{bio} with increasing N for the NOON state, optimal state, SIL, and HL cases show that the optimal states remai[n beyond](#page-4-0) the SIL, regardless of N for the nanowire. (d) Same as (c), but for the wedge waveguide. In both (c) and (d), the value of n_{bio} corresponds to point (2) in Figure 4c and d, respectively. The quantum enhancement in both plots (c and d) is reduced with increasing N, as the gap between the optimal state resolution and the SIL decreases with N. A line within the shad[ed area](#page-4-0) [sh](#page-4-0)ows an improvement over classical plasmonic sensing.

It is worth noting that the quantum dielectric case where losses are absent or nearly negligible, shown in Figure 2c, provides smaller a resolution $\delta n_{\rm bio}$ than the case of quantum plasmonic sensing including loss. However, this doe[s not mea](#page-2-0)n that the quantum dielectric case is always the best strategy because it is diffraction limited and cannot be used for a sensing on scales far below the operating wavelength. In such a scenario, the use of quantum resources in a plasmonic system would be the best strategy, although at the cost of the sensing resolution.

We also investigate the resolution δn_{bio} as N increases for the NOON state, the optimal state, the SIL, and the HL. These more general results are shown in Figure 5c,d, where the optimal states remain beyond the SIL (upper dashed line), regardless of N. It should be noted that the quantum enhancement is reduced with increasing N, that is, in Figure 5c,d, the gap between the HL and the SIL decreases with −

increasing *N*, $\delta n_{\text{bio}}^{(\text{SL})} - \delta n_{\text{bio}}^{(\text{HL})} = \frac{1}{\sqrt{N}} \left(\frac{1 + \sqrt{\eta}}{2\sqrt{\eta}} \right)$ $+\sqrt{\eta}$ 1 | $\partial \phi$ $n_{\text{bio}}^{\text{(SIL)}} - \delta n_{\text{bio}}^{\text{(HL)}} = \frac{1}{\sqrt{N}} \bigg(\frac{1 + \sqrt{\eta}}{2\sqrt{\eta}} - \frac{1}{\sqrt{N}} \bigg) \bigg| \frac{\partial}{\partial n}$ 2 $1 \Big| \frac{\partial \phi}{\partial t} \Big|^{-1}$ bio , while the optimal state resolution remains at a roughly fixed

distance below the SIL. On the other hand, the relative difference, defined by $(\delta n_{\rm bio}^{\rm (SIL)} - \delta n_{\rm bio}^{\rm (HL)})/\delta n_{\rm bio}^{\rm (SIL)}$, approaches unity in the limit of large N, while the other relative difference, defined by $(\delta n_{\text{bio}}^{(\text{SL})} - \delta n_{\text{bio}}^{(\text{HL})})/\delta n_{\text{bio}}^{(\text{HL})}$, diverges in the limit of large N. Such a behavior naturally arises from the \sqrt{N} improvement of the HL over the SIL. Considering Figure 5c,d, it might seem at first that quantum plasmonic sensing is not necessary because a given resolution can always be achieved by simply increasing the intensity of a classical input source to get the SIL, for example, $\delta n_{\rm bio} \sim 10^{-8}$ RIU is, in principle,

achievable by a $\lambda_0 = 810$ nm laser with an initial power of 1 mW having $N \sim 4 \times 10^{15}$ photons per second and an appropriate mode volume with a large power density.^{31,53,60} A high-power source, however, is not commonly desired for biological measurements since it may damage t[he](#page-6-0) [spe](#page-7-0)cimen under investigation^{60−62} or cause other unwanted phenomena such as thermal modulation of the surface plasmon mode. 63 In this case, at th[e few-](#page-7-0)photon level, one may then consider the benefits of using quantum sensing with either a di[elec](#page-7-0)tric or plasmonic waveguide. Here, for a fixed value of N, the quantum plasmonic sensor provides a low mode volume and allows one to go beyond the SIL in a compact setting below the diffraction limit. This is crucial when only a small biological sample is available, or one would like a more compact and integrated sensing device than standard dielectric components can achieve. Note that while the power density in a plasmonic waveguide is enhanced compared to a dielectric waveguide due to the low mode volume, it is the total power that is important in gaining the quantum advantage, as the shot-noise or Heisenberg limits are related to the photon number statistics rather than the optical power density. Despite all the demanding requirements of quantum measurement with plasmonic systems, in recent years several experimental studies have demonstrated the feasibility of quantum plasmonic sensing using low intensity input sources.^{28−30}

Discussion. In this work we studied quantum plasmonic sensing in the few photon regime and [show](#page-6-0)ed an example quantum plasmonic sensor that can beat the SNL in the presence of metallic losses. We have demonstrated how the inclusion of quantum techniques in a plasmonic system enables one to further improve its sensitivity and resolution beyond the SNL, while keeping the compactness of the device on scales far below the diffraction limit. Our analysis is applicable to any type of plasmonic sensing platform and we leave a variety of technical issues related to quantum plasmonic sensors for future works. For example, the performance of a quantum plasmonic sensor would benefit from further investigation into different excitation platforms such as a prism, grating, localized SPR sensor, metamaterials and graphene, as well as modulation-based approaches. In addition to the sensitivity and resolution considered in this work, other figures of merit such as accuracy, precision, or kinetic analysis will need to be taken into account for practical use in industry. We envisage that progress in quantum metrology will reshape the field of plasmonic biosensing, a field that has already developed into mature technology for at least two decades.³¹ Our work opens up a path between the quantum metrology and plasmonic sensing fields, and has the potential to l[ead](#page-6-0) to a variety of studies at the level of practical realization. Integrated quantum plasmonic sensors may also find application in on-chip nanoscale quantum network devices, with potential uses in quantum tasks where precise and compact measurement is required. $64,65$

■ AS[SOCI](#page-7-0)ATED CONTENT

6 Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphotonics.6b00082.

> [The characteristic equ](http://pubs.acs.org)ations for [the plasmonic and](http://pubs.acs.org/doi/abs/10.1021/acsphotonics.6b00082) [dielectr](http://pubs.acs.org/doi/abs/10.1021/acsphotonics.6b00082)ic nanowire waveguides, analytical expression of the quantum Fisher information in the presence of loss,

■ AUTHOR [INFO](http://pubs.acs.org/doi/suppl/10.1021/acsphotonics.6b00082/suppl_file/ph6b00082_si_001.pdf)RMATION

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